

Spin injection via (110)-grown semiconductor barriers

P. S. Alekseev, M. M. Glazov, and S. A. Tarasenko
A. F. Ioffe Physical-Technical Institute, 194021 St.-Petersburg, Russia

We study the tunneling of conduction electrons through a (110)-oriented single-barrier heterostructure grown from III-V semiconductor compounds. It is shown that, due to low spatial symmetry of such a barrier, the tunneling current through the barrier leads to an electron spin polarization. The inverse effect, generation of a direct tunneling current by spin polarized electrons, is also predicted. We develop the microscopic theory of the effects and show that the spin polarization emerges due to the combined action of the Dresselhaus spin-orbit coupling within the barrier and the Rashba spin-orbit coupling at the barrier interfaces.

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I. INTRODUCTION

The tunnel barriers play an important role in solid state physics. They determine the energy spectrum of coupled quantum wells and quantum dots, stability of charged impurities and excitons in electric field, miniband transport and Bloch oscillations in superlattices, etc., and underlie a number of electronic devices such as tunnel and resonant tunnel diodes [1, 2]. The tunnel barrier is an essential ingredient of a ferromagnet-semiconductor spin-injecting heterostructure which enables one to overcome the problem of the conductivity mismatch between the ferromagnet and semiconductor and achieve a high efficiency of spin injection [3–12]. About a decade ago, it was realized that the process of electron tunneling is spin dependent itself due spin-orbit interaction which couples spin states with the orbital motion. It was shown that the Rashba spin-orbit coupling at interfaces as well as the Dresselhaus coupling in the bulk of barrier make the barrier tunnel transmission dependent of the spin orientation and wave vector of incident electrons [13–16]. The effect of spin-dependent tunneling was proposed to be applied for the pure electric injection and detection of spin polarized carriers [17–29]. In the case of Rashba and Dresselhaus coupling in (001)-grown barriers in bulk semiconductors, the spin polarization of transmitted electrons linearly scales with the lateral component \mathbf{k}_{\parallel} of the electron wave vector and is of opposite sign for the wave vectors \mathbf{k}_{\parallel} and $-\mathbf{k}_{\parallel}$ [13, 15]. Therefore, the proposed methods of spin injection require the application of an additional, lateral, electric field which causes the electron drift in the interface plane and makes the electron distribution in the \mathbf{k}_{\parallel} space anisotropic.

In this paper, we show that the spin injection via tunnel structures in bulk semiconductors can be achieved even for isotropic in the interface plane electron distribution. Such an effect occurs for barriers of sufficiently low spatial symmetry only being not allowed, e.g., in (001)-grown structures. Microscopically, it is caused by the combined action of the Dresselhaus spin-orbit coupling in the barrier and the Rashba spin-orbit coupling at the barrier interfaces. To be specific, we consider single-barrier tunnel structures with the (110) crystallographic orienta-

tion and present an analytical theory of the spin injection.

II. MICROSCOPIC MODEL

Consider a zinc-blende-type semiconductor heterostructure with the symmetric potential barrier grown along the $z \parallel [110]$ axis, see Fig. 1. Electrons with different incident wave vectors $\mathbf{k} = (k_x, k_y, k_z)$ tunnel through the barrier, where k_x and k_y are projections of the wave vector onto the in-plane axes $x \parallel [1\bar{1}0]$ and $y \parallel [00\bar{1}]$. The effective Hamiltonian describing electron states in the conduction band has the form

$$\mathcal{H} = \mathcal{H}_0 + \mathcal{H}_R + \mathcal{H}_D, \quad (1)$$

where \mathcal{H}_0 is the spin-independent contribution,

$$\mathcal{H}_0 = \frac{\hbar^2(k_x^2 + k_y^2)}{2m(z)} - \frac{\hbar^2}{2} \frac{\partial}{\partial z} \frac{1}{m(z)} \frac{\partial}{\partial z} + V(z), \quad (2)$$

$m(z)$ is the effective mass, which may be different inside and outside the barrier, $V(z)$ is the heteropotential, $V(z) = V_0 > 0$ if $0 < z < a$ and $V(z) = 0$ elsewhere, a is the barrier thickness, \mathcal{H}_R is the Rashba spin-orbit coupling at interfaces

$$\mathcal{H}_R = \alpha [\delta(z - a) - \delta(z)] (\sigma_x k_y - \sigma_y k_x), \quad (3)$$

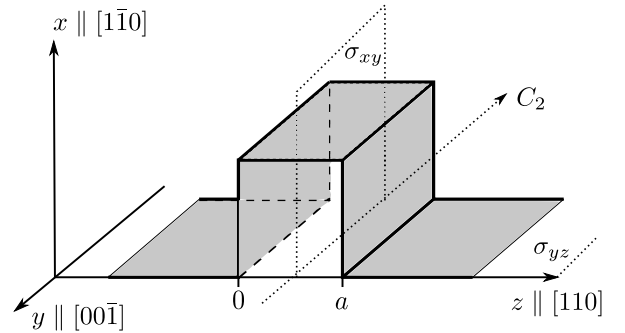


FIG. 1: The sketch of a symmetric tunnel barrier with the (110) crystallographic orientation. The point-group symmetry elements of the structure includes the two-fold rotation axis $C_2 \parallel y$ and the mirror planes σ_{xy} and σ_{yz} .

α is the parameter determined by the band offsets, σ_j ($j = x, y, z$) are the Pauli matrices, and \mathcal{H}_D is the Dresselhaus spin-orbit coupling. In the chosen coordinate frame, \mathcal{H}_D can be presented as the sum of four terms

$$\mathcal{H}_{D1} = i \frac{\sigma_x}{2} \left\{ \gamma(z), \frac{\partial^3}{\partial z^3} \right\}_{\text{sym}}, \quad (4)$$

$$\mathcal{H}_{D2} = \frac{\sigma_z k_x}{2} \frac{\partial}{\partial z} \gamma(z) \frac{\partial}{\partial z}, \quad (5)$$

$$\mathcal{H}_{D3} = i \left[\sigma_x \left(\frac{k_x^2}{2} + k_y^2 \right) - 2\sigma_y k_x k_y \right] \left\{ \gamma(z), \frac{\partial}{\partial z} \right\}_{\text{sym}}, \quad (6)$$

$$\mathcal{H}_{D4} = \sigma_z k_x \left(\frac{k_x^2}{2} - k_y^2 \right) \gamma(z), \quad (7)$$

where $\gamma(z)$ is the bulk Dresselhaus parameter and the notation $\{\dots\}_{\text{sym}}$ denotes the operator symmetrization. The terms \mathcal{H}_{D1} , \mathcal{H}_{D2} , \mathcal{H}_{D3} , and \mathcal{H}_{D4} contain the derivative of the third, second, first, and zero order, respectively. We assume the kinetic energy of electrons to be substantially smaller than the barrier height V_0 and, therefore, neglect the terms \mathcal{H}_{D3} and \mathcal{H}_{D4} in comparison with \mathcal{H}_{D1} and \mathcal{H}_{D2} , respectively.

We are interested in the total spin polarization proportional to the tunneling current through the barrier j_z . In (110)-grown structures, such an effect is allowed by symmetry and phenomenologically given by

$$s_x(z) \propto j_z, \quad (8)$$

where $s_x(z)$ is the steady-state spin density. Indeed, symmetric (110)-grown barriers are described by the C_{2v} point group which consists of the two-fold rotation axis $C_2 \parallel y$, two mirror planes $\sigma_{xy} \parallel (110)$ and $\sigma_{yz} \parallel (\bar{1}\bar{1}0)$, and the identity element [30], as shown in Fig. 1. In this point group, the vector component j_z and pseudovector component s_x belong to the same irreducible representation, i.e., under all symmetry operations of the group they transform in a similar way [31]. Therefore, the symmetry allows the linear coupling of s_x and j_z and imposes the condition that the current-induced spin density $s_x(z)$ is an even function with respect to the barrier center. The latter suggests that the electrons transmitted through the barrier and those reflected from the barrier have the same spin polarization. Note that, in (001)-grown structures, the spin injection is absent for the tunneling current along the barrier normal and may occur only in the presence of the lateral component of the current. Equation (8) also shows the possibility of the inverse effect: A non-equilibrium spin polarization of carriers along the x axis causes the direct current through the barrier.

We assume that the electrons incident upon the barrier are unpolarized and their distribution in the interface plane is isotropic. Symmetry analysis of the spin-orbit terms shows that the spin injection given by Eq. (8)

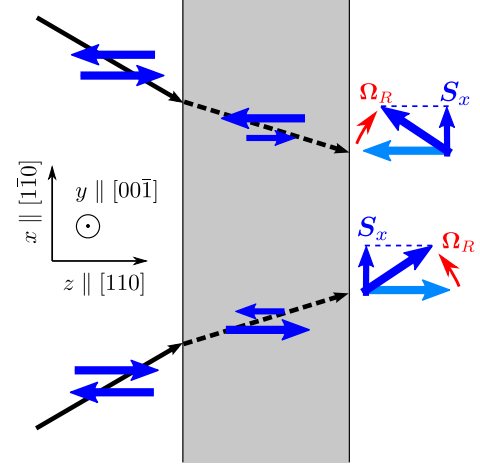


FIG. 2: (Color online) The model of spin injection via (110)-grown barrier. The spin component $S_x > 0$ of electrons transmitted through the barrier with different in-plane wave vectors emerges due to (i) anisotropic spin filtering caused by the Dresselhaus spin-orbit coupling in the barrier interior followed by (ii) spin rotation in the interface-induced Rashba effective magnetic field Ω_R .

can be microscopically related to (i) joint action of the Rashba \mathcal{H}_R and Dresselhaus \mathcal{H}_{D2} terms or (ii) solely \mathcal{H}_{D1} term. The calculation based on the perturbation theory demonstrates that the term \mathcal{H}_{D1} does not lead to a spin injection, see Appendix and Ref. [25]. Therefore, we focus below on the mechanism caused by the joint action of the Rashba spin-orbit coupling at interfaces and Dresselhaus coupling in the barrier bulk.

The mechanism of the spin injection can be viewed as a two-step process illustrated in Fig. 2. At the first stage, unpolarized electrons with different in-plane wave vectors k_x are incident upon the barrier and tunnel through it being affected by the Dresselhaus spin-orbit coupling. The term \mathcal{H}_{D2} can be considered as the spin-dependent correction to the effective mass along z which is proportional to k_x , compare Eqs. (2) and (5). Due to the fact that the barrier transmission probability depends on the effective mass, the electrons at the exit from the barrier gain the spin polarization $S_z \propto k_x$. Similar mechanism of anisotropic spin filtering caused by the Dresselhaus coupling for (001)-grown structures was considered in Refs. [15, 20]. Note that, for the equal population of the k_x and $-k_x$ states, the net spin polarization of electrons is absent at this step. The net spin polarization emerges at the second stage due to the action of the Rashba spin-orbit coupling at the interface, see Eq. (3). The Rashba coupling can be considered as an effective magnetic field Ω_R lying in the interface plane which causes the spin rotation. The y -component of the effective field Ω_R is proportional to k_x , therefore, the rotation axes are opposite for the electrons with positive and negative k_x . As a result, the rotation leads to the spin component $S_x > 0$ for all the electrons transmitted through the barrier. The value of the net spin polarization is determined by the

efficiency of anisotropic spin filtering in the barrier bulk and the spin rotation angle at the interface. We note that similar mechanism leads to the spin polarization of electrons reflected from the barrier.

III. THEORY

The theory of spin injection can be conveniently developed by using the spin-dependent transfer matrix technique. The 4×4 transfer matrix \mathcal{P} through the whole tunnel structure relates the spinor wave function Ψ and its derivative $\Psi' = d\Psi/dz$ at $z = -0$ to those at $z = a+0$,

$$\begin{pmatrix} \Psi(a+0) \\ \Psi'(a+0) \end{pmatrix} = \mathcal{P} \begin{pmatrix} \Psi(-0) \\ \Psi'(-0) \end{pmatrix}, \quad \mathcal{P} = \begin{pmatrix} P_{\psi\psi} & P_{\psi\psi'} \\ P_{\psi'\psi} & P_{\psi'\psi'} \end{pmatrix}, \quad (9)$$

where $P_{\psi\psi}$, $P_{\psi\psi'}$, $P_{\psi'\psi}$, and $P_{\psi'\psi'}$ are 2×2 matrices. Higher-order derivatives of the wave function are expressed via Ψ and Ψ' because the Schrödinger equation with the Hamiltonian $\mathcal{H}_0 + \mathcal{H}_{D2} + \mathcal{H}_R$ is a differential equation of the second order in z . By definition, the matrix \mathcal{P} can be presented as the ordered product of the transfer matrices through individual parts of the structure,

$$\mathcal{P} = \mathcal{P}^{(r)} \mathcal{P}^{(b)} \mathcal{P}^{(l)}, \quad (10)$$

where $\mathcal{P}^{(l/r)}$ is the transfer matrix through the left/right interface and $\mathcal{P}^{(b)}$ is the transfer matrix through the barrier interior.

Solution of the Schrödinger equation at the left interface with the standard boundary conditions, which follow from the Hamiltonian $\mathcal{H}_0 + \mathcal{H}_{D2} + \mathcal{H}_R$ and require the continuity of Ψ and $(1/m - \gamma\sigma_z k_x/\hbar^2)\Psi'$, shows that the transfer matrix $\mathcal{P}^{(l)}$ has the components

$$P_{\psi\psi}^{(l)} = I, \quad P_{\psi\psi'}^{(l)} = 0, \quad (11a)$$

$$P_{\psi'\psi}^{(l)} = -\frac{2m_2\alpha}{\hbar^2} \left(I - \frac{m_2\gamma_2}{\hbar^2} \sigma_z k_x \right)^{-1} (\sigma_x k_y - \sigma_y k_x), \quad (11b)$$

$$P_{\psi'\psi'}^{(l)} = \frac{m_2}{m_1} \left(I - \frac{m_2\gamma_2}{\hbar^2} \sigma_z k_x \right)^{-1} \left(I - \frac{m_1\gamma_1}{\hbar^2} \sigma_z k_x \right), \quad (11c)$$

where m_2 and γ_2 are the effective mass and Dresselhaus constant inside the barrier, m_1 and γ_1 are those outside the barrier, and I is the 2×2 unit matrix. The transfer matrix through the right interface $\mathcal{P}^{(r)}$ is equal to the inverse transfer matrix through the left interface, $\mathcal{P}^{(l)-1}$, and readily obtained from Eqs. (11) by the replacement $\alpha \rightarrow -\alpha$, $m_{1(2)} \rightarrow m_{2(1)}$, and $\gamma_{1(2)} \rightarrow \gamma_{2(1)}$. The transfer matrix through the barrier interior with the term \mathcal{H}_{D2} included in the Hamiltonian is given by

$$P_{\psi\psi}^{(b)} = P_{\psi'\psi'}^{(b)} = \begin{pmatrix} \cosh q_+ a & 0 \\ 0 & \cosh q_- a \end{pmatrix}, \quad (12a)$$

$$P_{\psi\psi'}^{(b)} = \begin{pmatrix} q_+^{-1} \sinh q_+ a & 0 \\ 0 & q_-^{-1} \sinh q_- a \end{pmatrix}, \quad (12b)$$

$$P_{\psi'\psi}^{(b)} = \begin{pmatrix} q_+ \sinh q_+ a & 0 \\ 0 & q_- \sinh q_- a \end{pmatrix}, \quad (12c)$$

where

$$q_{\pm} = q \left(1 \pm \frac{\gamma_2 m_2 k_x}{\hbar^2} \right)^{-1/2} \quad (13)$$

and

$$q = \sqrt{\frac{2m_2 V_0}{\hbar^2} - k_z^2 \frac{m_2}{m_1} - k_{\parallel}^2 \left(\frac{m_2}{m_1} - 1 \right)} \quad (14)$$

with $k_{\parallel} = \sqrt{k_x^2 + k_y^2}$ being the in-plane wave vector. The inverse matrix $\mathcal{P}^{(b)-1}$ is obtained from $\mathcal{P}^{(b)}$ by the replacement $a \rightarrow -a$.

The knowledge of the transfer matrix \mathcal{P} allows one to calculate the spin-dependent coefficient of electron transmission and reflection from the tunnel structure. Assuming that the spin-orbit interaction is negligible outside the barrier and electrons are incident upon the structure from the left, we present the wave function describing the incident, reflected, and transmitted waves in the form

$$\psi_{\mathbf{k}}(\mathbf{r}) = \begin{cases} \chi e^{i\mathbf{k}_{\parallel} \cdot \boldsymbol{\rho} + ik_z z} + \mathcal{R}_{\mathbf{k}} \chi e^{i\mathbf{k}_{\parallel} \cdot \boldsymbol{\rho} - ik_z z}, & z < 0, \\ \mathcal{T}_{\mathbf{k}} \chi e^{i\mathbf{k}_{\parallel} \cdot \boldsymbol{\rho} + ik_z(z-a)}, & z > a \end{cases} \quad (15)$$

where χ is the incident electron spinor, $\mathcal{R}_{\mathbf{k}}$ and $\mathcal{T}_{\mathbf{k}}$ are 2×2 matrices of amplitude reflection and transmission coefficients. It follows from Eqs. (9) and (15) that the matrices $\mathcal{R}_{\mathbf{k}}$ and $\mathcal{T}_{\mathbf{k}}$ satisfy the equation

$$\begin{pmatrix} \mathcal{T}_{\mathbf{k}} \\ ik_z \mathcal{T}_{\mathbf{k}} \end{pmatrix} = \mathcal{P} \begin{pmatrix} I + \mathcal{R}_{\mathbf{k}} \\ ik_z (I - \mathcal{R}_{\mathbf{k}}) \end{pmatrix}, \quad (16)$$

which yields

$$\mathcal{R}_{\mathbf{k}} = -(\mathcal{P}_{\psi\psi} + \mathcal{P}_{\psi'\psi'} - ik_z \mathcal{P}_{\psi\psi'} + ik_z^{-1} \mathcal{P}_{\psi'\psi})^{-1} \quad (17)$$

$$\times (\mathcal{P}_{\psi\psi} - \mathcal{P}_{\psi'\psi'} + ik_z \mathcal{P}_{\psi\psi'} + ik_z^{-1} \mathcal{P}_{\psi'\psi}),$$

$$\mathcal{T}_{\mathbf{k}} = 2(\bar{\mathcal{P}}_{\psi\psi} + \bar{\mathcal{P}}_{\psi'\psi'} + ik_z \bar{\mathcal{P}}_{\psi\psi'} - ik_z^{-1} \bar{\mathcal{P}}_{\psi'\psi})^{-1}, \quad (18)$$

where $\bar{\mathcal{P}} = \mathcal{P}^{-1}$, i.e., $\bar{\mathcal{P}}_{\psi\psi}$, $\bar{\mathcal{P}}_{\psi\psi'}$, $\bar{\mathcal{P}}_{\psi'\psi}$, and $\bar{\mathcal{P}}_{\psi'\psi'}$ are the 2×2 blocks of the inverse transfer matrix. Since $\mathcal{P} = \mathcal{P}^{(r)} \mathcal{P}^{(b)} \mathcal{P}^{(l)}$, $\mathcal{P}^{(l)-1} = \mathcal{P}^{(r)}$, $\mathcal{P}^{(r)-1} = \mathcal{P}^{(l)}$, and $\mathcal{P}^{(b)-1}(a) = \mathcal{P}^{(b)}(-a)$, the inverse transfer matrix through the structures is given by $\mathcal{P}^{-1}(a) = \mathcal{P}(-a)$. It follows that the amplitude coefficients of transmission and reflection for the electrons incident upon the barrier from the right (with $k_z < 0$) are obtained from $\mathcal{T}_{\mathbf{k}}$ and $\mathcal{R}_{\mathbf{k}}$, respectively, by the replacement $a \rightarrow -a$.

A. Spin injection

The spin of electrons with the wave vector \mathbf{k} transmitted through the barrier is given by

$$\mathbf{S}_{\mathbf{k}} = \frac{\text{Tr}(\boldsymbol{\sigma} g_{\mathbf{k}})}{2\text{Tr}(g_{\mathbf{k}})}, \quad (19)$$

where $g_{\mathbf{k}}$ is the 2×2 spin matrix describing the charge and spin fluxes of the transmitted particles. In the case when the electrons incident upon the barrier are unpolarized, the matrix $g_{\mathbf{k}}$ has the form [18]

$$g_{\mathbf{k}} = \mathcal{T}_{\mathbf{k}} \mathcal{T}_{\mathbf{k}}^\dagger f_{\mathbf{k}} v_z \Theta(v_z), \quad (20)$$

where $f_{\mathbf{k}}$ is the distribution function of incident electrons, $v_z = \hbar k_z / m_1$ is the velocity component along the barrier normal, and $\Theta(v_z)$ is the Heaviside step function. Note that the matrix describing the flux of reflected electrons (with $k_z < 0$) is obtained from Eq. (20) by the replacement $\mathcal{T}_{\mathbf{k}} \rightarrow \mathcal{R}_{\mathbf{k}}$ and $k_z \rightarrow -k_z$.

The equations presented above enable one to calculate the spin polarization of transmitted and reflected electrons for given parameters of the tunnel structure. To simplify the calculation, we assume that the effective masses inside and outside the barrier are the same ($m_1 = m_2 = m$) and neglect the spin-orbit coupling outside the barrier ($\gamma_2 = \gamma$, $\gamma_1 = 0$). In this case, to first order in α , γ , and $\alpha\gamma$, the matrix $\mathcal{T}_{\mathbf{k}}$ has the form

$$\mathcal{T}_{\mathbf{k}} = \left[I + \frac{\gamma m c_1}{4\hbar^2} \sigma_z k_x + \frac{\alpha \gamma m^2 c_2}{\hbar^4 q} (\sigma_x k_x + \sigma_y k_y) k_x \right] t_{\mathbf{k}}, \quad (21)$$

where c_1 and c_2 are the coefficients given by

$$c_1 = [iqa(k_z/q - q/k_z) \cosh qa - (2qa + 3k_z/q + 3q/k_z) \sinh qa] t_{\mathbf{k}}, \quad (22a)$$

$$c_2 = [(3i + q^2 a/k_z) \sinh qa - iqa \cosh qa] t_{\mathbf{k}}, \quad (22b)$$

and $t_{\mathbf{k}}$ is the amplitude transmission coefficient in the absence of spin-orbit coupling,

$$t_{\mathbf{k}} = \left[\cosh qa + \frac{i}{2} \left(\frac{q}{k_z} - \frac{k_z}{q} \right) \sinh qa \right]^{-1}. \quad (23)$$

Then, the symmetric part of the spin distribution of transmitted electrons assumes the form

$$S_{\mathbf{k},x}^{(\text{sym})} = 2 \frac{\alpha \gamma m^2 k_x^2 k_z}{\hbar^4} \times \frac{3(q^2 - k_z^2) \sinh^2 qa + qa(k_z^2 + q_0^2) \cosh qa \sinh qa}{(k_z^2 + q^2)^2 \cosh^2 qa - (k_z^2 - q^2)^2}. \quad (24)$$

In the particular case of high and thick enough barrier, $qa \gg 1$ and $q \gg k_z$, Eq. (24) is simplified to

$$S_{\mathbf{k},x}^{(\text{sym})} = 2 \frac{\alpha \gamma m^2 k_x^2 k_z a}{\hbar^4 q}. \quad (25)$$

The spin distribution (24) is an even function of the in-plane wave vector, therefore, the spin injection via (110)-grown tunnel barriers occur even for isotropic in the interface plane distribution of incident electrons.

Finally, we estimate the efficiency of spin injection. We consider the potential barrier of the width $a = 100 \text{ \AA}$ and height $V_0 = 200 \text{ meV}$ based on the GaSb/Al_{0.17}Ga_{0.83}Sb heterostructure and take the bulk GaSb parameters [32]: $m = 0.041m_0$, with m_0 being the free electron mass, and $\gamma = 186 \text{ eV} \cdot \text{\AA}^3$. The interface Rashba coefficient is estimated [34, 35] as $\alpha \approx (P^2/3) \{ \Delta_1 / [(E - E_{\Gamma_8}^{(1)})(E - E_{\Gamma_7}^{(1)})] - \Delta_2 / [(E - E_{\Gamma_8}^{(2)})(E - E_{\Gamma_7}^{(2)})] \}$, where P is the Kane matrix element, E is the electron energy, $\Delta_j = E_{\Gamma_8}^{(j)} - E_{\Gamma_7}^{(j)}$, $E_{\Gamma_8}^{(j)}$ and $E_{\Gamma_7}^{(j)}$ are the energies of the Γ_8 and Γ_7 valence bands at $\mathbf{k} = 0$ outside ($j = 1$) and inside ($j = 2$) the barrier. This yields $\alpha \approx 2.5 \text{ eV} \cdot \text{\AA}^2$ for the Kane matrix element in GaSb $P = 9.7 \text{ eV}$, the band gap 0.81 eV , the valence band offset $\approx 70 \text{ meV}$ and $\Delta_1 = \Delta_2 \approx 0.76 \text{ eV}$, the above parameters are from Refs. [32, 33]. Then, for the wave vectors $k_x = k_z = 2 \times 10^6 \text{ cm}^{-1}$, the spin polarization $P_s = 2|S_x|$ of electrons transmitted through the barrier can be estimated as 0.1%. This value is not high, however, well above the spin polarization detectable in experiments. The efficiency of spin injection can be enhanced in multiple-barrier structures provided spin relaxation processes are slow enough.

B. Spin-galvanic effect

Besides the spin polarization induced by tunneling current through the barrier, one can consider the inverse effect, namely, the emergence of a direct electric current through the barrier in the presence of spin polarization, which is also possible in (110)-grown structures. Now we assume that the tunnel structure is initially unbiased but electrons at the both sides of the barrier are spin polarized along the x axis. Due to spin-orbit coupling, the barrier transparency for the electrons incident on the barrier from the left with the initial spin polarization S_x is different from that for the electrons incident of the barrier from the right. As a result, the oppositely directed electron fluxes do not compensate each other which leads to a direct electric current through the barrier.

Taking into account that the transmission coefficients for the electrons incident upon the barrier from the left and the right are connected to each other by the formal replacement $a \rightarrow -a$ [see discussion after Eqs. (17) and (18)], one can write for the tunneling current density

$$j_z = e \sum_{\mathbf{k}} \text{Tr}[\mathcal{T}_{\mathbf{k}}(a) \rho_l \mathcal{T}_{\mathbf{k}}^\dagger(a)] v_z \Theta(v_z) + e \sum_{\mathbf{k}} \text{Tr}[\mathcal{T}_{\mathbf{k}}(-a) \rho_r \mathcal{T}_{\mathbf{k}}^\dagger(-a)] v_z \Theta(-v_z), \quad (26)$$

where ρ_l and ρ_r are the electron spin-density matrices on the left-hand and right-hand sides of the structure [18].

For the same electron distribution at both side of the structure described by the distribution function $f(\varepsilon)$, where ε is the electron energy, and small degree of spin polarization p_s along the x axis, the density matrices are given by

$$\rho_l = \rho_r = f(\varepsilon)I - \frac{df(\varepsilon)}{d\varepsilon} \frac{2p_s\sigma_x}{\langle 1/\varepsilon \rangle}, \quad (27)$$

where $\langle 1/\varepsilon \rangle$ is the mean value of the reciprocal kinetic energy, which is equal to $3/E_F$ for three-dimensional degenerate electron gas with the Fermi energy E_F and $2/(k_B T)$ for nondegenerate gas at the temperature T . The calculation of the tunneling current Eq. (26) with the transmission coefficient (21) and the density matrices (27) yields

$$j_z = -8 \frac{e\alpha\gamma m^2 p_s}{\langle 1/\varepsilon \rangle \hbar^4} \sum_{\mathbf{k}} \frac{df(\varepsilon)}{d\varepsilon} \frac{k_x^2 v_z}{q} |t_{\mathbf{k}}|^2 \text{Re}(c_2). \quad (28)$$

Finally, for the degenerate electron gas at the both sides of the barrier, the high and thick barrier, $q \gg k_F$, $qa \gg 1$, and $k_F^2 a/q \ll 1$, we derive

$$j_z = \frac{64ep_s}{105\pi^2} \frac{\alpha\gamma m a k_F^9}{\hbar^3 \kappa^3} \exp(-2\kappa a), \quad (29)$$

where k_F is the Fermi wave vector and $\kappa = \sqrt{2mV_0/\hbar^2}$. The estimation following Eq. (29) gives $j_z \sim 2$ mA/cm² for the single barrier of the width $a = 100\text{\AA}$ and height $V_0 = 200$ meV based on GaSb/Al_{0.17}Ga_{0.83}Sb, the Fermi wave vector $k_F = 2 \times 10^6$ cm⁻¹, and the spin polarization $p_s = 10\%$. Electric currents of a such density are reliably detectable in experiments.

IV. SUMMARY

We have developed the analytical theory of electron spin injection through non-magnetic semiconductor barriers with the (110) crystallographic orientation. The calculations are carried out by using the spin-dependent transfer matrix technique. It is shown that the tunneling of electrons through the barrier, which are described by an isotropic momentum distribution in the interface plane, results in their partial spin polarization along the $[1\bar{1}0]$ axis. The microscopic mechanism of the spin polarization is a two-step process comprising spin filtering due to Dresselhaus spin-orbit coupling in the barrier interior and the spin rotation in the Rashba effective magnetic field at the interfaces. The inverse effect, emergence of a direct tunneling current through the barrier due to spin polarization of carriers, is also described. The spin-dependent tunneling phenomenon could be employed for designing pure electric spin injectors and detectors.

Acknowledgments

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Appendix A: Effect of \mathcal{H}_{D1} on tunneling

The \mathbf{k} -cubic spin-orbit splitting of the conduction band is valid for small wave vectors and should be treated as a perturbation only. In particular, the term \mathcal{H}_{D1} contains the operator $\partial^3/\partial z^3$, therefore, the Schrödinger equation with the Hamiltonian $\mathcal{H}_0 + \mathcal{H}_{D1}$ in the barrier would have the basic solutions $\propto \exp(q_z z)$ with three different q_z for a given electron energy. One of the solutions is a rapidly oscillating function with $|q_z| \propto \gamma^{-1}$, it is unphysical and beyond of the effective Hamiltonian approximation. Besides, the operator \mathcal{H}_{D1} is not Hermitian for the class of wave functions of heterostructures with abrupt interfaces. Therefore, the conventional procedure of calculating the transmission and reflection coefficients by constructing the basis solutions of the Schrödinger equation in each layer of the structure and using boundary conditions at interfaces become ambiguous. Instead, we analyze the effect of spin-orbit coupling \mathcal{H}_{D1} on tunneling in the framework of perturbation theory. Since the term \mathcal{H}_{D1} does not contain the in-plane wave vector, we assume for simplicity that $k_x, k_y = 0$ and consider one-dimensional case.

In the absence of spin-orbit coupling, the wave functions used in the theory of electron tunneling through a rectangular barrier are given by

$$\psi_k^{(+)}(z) = \begin{cases} e^{ikz} + r_k e^{-ikz}, & z < 0, \\ A_k e^{qz} + B_k e^{-qz}, & 0 < z < a, \\ t_k e^{ik(z-a)}, & z > a, \end{cases} \quad (A1)$$

where t_k and r_k are the amplitude transmission and reflection coefficients [cf. Eq. (23)],

$$t_k = \left[\cosh qa + \frac{i}{2} \left(\frac{q}{k} - \frac{k}{q} \right) \sinh qa \right]^{-1}, \quad (A2)$$

$$r_k = -\frac{i}{2} \left[\frac{q}{k} + \frac{k}{q} \right] \sinh(qa) t_k,$$

A and B are the function amplitudes in the barrier,

$$A_k = \frac{t_k}{2} \left(1 + i \frac{k}{q} \right) e^{-qa}, \quad B_k = \frac{t_k}{2} \left(1 - i \frac{k}{q} \right) e^{qa}, \quad (A3)$$

$k = \sqrt{2mE/\hbar^2} > 0$ is the initial wave vector, $q = \sqrt{2m(V_0 - E)/\hbar^2}$, and we assume that the effective masses inside and outside the barrier coincide. In terms of the scattering problem, the wave function $\psi_k^{(+)}$ at $|z| > a$ represents the sum of the incident wave and the wave diverging from the barrier. Besides the functions $\psi_k^{(+)}$, one can formally consider another type of the Schrödinger equation solutions which at $|z| > a$ describe

the sum of the incident and converging waves. The corresponding wave functions can be presented in the form

$$\psi_k^{(-)}(z) = \begin{cases} t_k^* e^{ikz}, & z < 0, \\ B_k^* e^{q(z-a)} + A_k^* e^{-q(z-a)}, & 0 < z < a, \\ e^{ik(z-a)} + r_k^* e^{-ik(z-a)}, & z > a. \end{cases} \quad (\text{A4})$$

Exploiting the analogy between the theory of tunneling and the theory of quantum scattering [36, 37], we obtain the first-order correction to the amplitude transmission coefficient caused by the Hermitian perturbation \mathcal{H}_{D1} ,

$$\delta t_k = -\frac{im}{\hbar^2 k} \langle \psi_k^{(-)} | \mathcal{H}_{D1} | \psi_k^{(+)} \rangle. \quad (\text{A5})$$

To calculate δt_k we take into account that the functions $\psi_k^{(\pm)}$ satisfy the Schrödinger equation with the Hamiltonian \mathcal{H}_0 and the symmetrization in Eq. (4) can be done in one of two possible ways:

$$\left\{ \gamma(z), \frac{\partial^3}{\partial z^3} \right\}_{\text{sym}} = \frac{1}{2} \frac{\partial}{\partial z} \left[\gamma(z) \frac{\partial}{\partial z} + \frac{\partial}{\partial z} \gamma(z) \right] \frac{\partial}{\partial z} \quad (\text{A6a})$$

or

$$\left\{ \gamma(z), \frac{\partial^3}{\partial z^3} \right\}_{\text{sym}} = \frac{1}{2} \left[\gamma(z) \frac{\partial^3}{\partial z^3} + \frac{\partial^3}{\partial z^3} \gamma(z) \right]. \quad (\text{A6b})$$

For the both types of symmetrization, the calculation

yields the same result

$$\delta t_k = \frac{\sigma_x m^2}{2\hbar^4 k} \int \gamma(z) [V(z) - E] \left[\psi_k^{(-)*} \psi_k^{(+)' } - \psi_k^{(-)'} \psi_k^{(+)} \right] dz, \quad (\text{A7})$$

where $\psi_k^{(\pm)'} = d\psi_k^{(\pm)}/dz$. In the limiting case of rectangular barrier with the spin-orbit splitting of electron states in the barrier given by \mathcal{H}_{D1} , the correction to amplitude transmission coefficient assumes the form

$$\delta t_k = \frac{i\sigma_x}{2} \frac{\gamma m q^2 a}{\hbar^2} t_k. \quad (\text{A8})$$

The probability for an electron with the spin projection $s_x = \pm 1/2$ to tunnel through the barrier is given by $|\langle s_x | t_k + \delta t_k | s_x \rangle|^2$. To first order in γ , where the above consideration is valid, the probability is independent of the spin orientation since $\text{Re}(t_k \delta t_k^*) \equiv 0$. Therefore, the \mathcal{H}_{D1} spin-orbit coupling does not lead to a spin polarization of electrons transmitted through the barrier. However, the correction δt_k results in the spin-dependent phase shift of the wave function which can be revealed in interference experiments. Similar conclusions on the effect of the term \mathcal{H}_{D1} on tunneling were made in Refs. [25, 38] by considering an imaginary correction to q .

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